

INDIAN MARITIME UNIVERSITY
(A Central University Government of India)
END SEMESTER EXAMINATIONS- JUNE 2019
DIPLOMA IN NAUTICAL SCIENCE
SEMESTER - I
APPLIED MATHEMATICS (UD11T2101)

Date: 24-06-2019
 Time: 02 hours

Max. Marks: 70
 Pass Marks: 35

Note : Attempt any 5 questions. Use of calculator is permitted.

Q.1. a) By vector method, find the area of the triangle whose vertices are $(3, -1, 2)$, $(1, -1, 3)$ and $(4, -3, 1)$. (7 marks)

b) If \vec{a} , \vec{b} and \vec{c} are non coplanar vectors then prove that $2\vec{a} - 4\vec{b} + 4\vec{c}$, $\vec{a} - 2\vec{b} + 4\vec{c}$ and $-\vec{a} + 2\vec{b} + 4\vec{c}$ are collinear. (7 marks)

Q.2. a) A man is known to speak truth 3 out of 4 times. He throws a die and reports that it is a six. Find the probability that it is actually a six. (7 marks)

b) Calculate the rank correlation coefficient from the following data showing the ranks of 10 students in 2 subjects

Navigation	3	8	9	2	7	10	4	6	1	5
Cargo	5	9	10	1	8	7	3	4	2	6

(7 marks)

Q.3. a) Find the equation of the circle passing to the point of intersection of the lines $3x - 2y - 1 = 0$ and $4x + y - 27 = 0$ and whose centre is the point $(3, -2)$. (7 marks)

b) Find the equation of ellipse whose focus is the point $(-1, 1)$ and the corresponding directrix is the line $x - y + 3 = 0$ and eccentricity is $\frac{1}{2}$. (7 marks)

Q.4. a) Evaluate $\int_0^1 \frac{1}{1+x^2} dx$ using Simpson's $1/3^{\text{rd}}$ rule dividing the interval $(0, 1)$ into 4 equal parts. (7 marks)

b) Metallic spheres of radii 6 cm, 8 cm and 10 cm, respectively, are melted to form a single solid sphere. Find the radius of the resulting sphere. (7 marks)

Q.5. The angles of elevation of the top of the tower from two points at a distance of 4m and 9m from the base of the tower and in a same line with

it are complimentary. Prove that the height of the tower is 6m. (14 marks)

Q.6. a) In a spherical ΔABC , $A = 88^{\circ}36'$, $B = 121^{\circ} 36.5'$ and $C = 69^{\circ} 34.5'$, find c . (7 marks)

b) In a spherical ΔPXY , $p = 53^{\circ} 20'$, $X = 92^{\circ} 05'$ and $Y = 90^{\circ}$ calculate P & y . (7 marks)

Q.7. a) Given $f(-2) = 46$, $f(-1) = 4$, $f(1) = 4$, $f(3) = 156$ and $f(4) = 484$, use the Lagrange interpolation formula to compute $f(0)$. (14 marks)